

## 1-out-of-2 Signature

Mirosław  
Kutyłowski<sup>1</sup>  
and  
Jun Shao<sup>2</sup>

What's  
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Definitions of  
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Our proposal

Extension

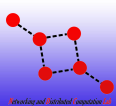
# 1-out-of-2 Signature

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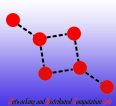
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# Signature with delegation capability

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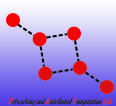
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In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.



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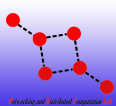
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In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature



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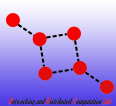
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In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature
- Proxy re-signature



# Signature with delegation capability

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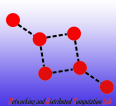
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In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature
- Proxy re-signature
- Mediated signature



# Signature with delegation capability

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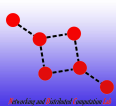
Our proposal

Extension

In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature

- In a proxy signature scheme, the original signer delegates his/her signing rights to a proxy, who can sign messages on behalf of the original signer afterwards.



# Signature with delegation capability

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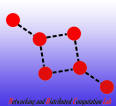
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Extension

In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature
- Proxy re-signature
  - In a proxy re-signature scheme, a proxy can transform a signature of the delegatee to another signature of the delegator on the same message.





# Signature with delegation capability

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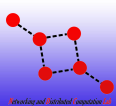
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Extension

In digital signature, when the signer is absent, he/she will delegate his/her signing rights to a proxy.

- Proxy signature
- Proxy re-signature
- Mediated signature
  - In a mediated signature scheme, an on-line semi-trusted mediator (SEM) should involve in every signing process to help the original signer to generate the signature.



# Scenario

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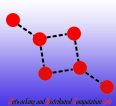
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Extension

In some cases, the signer just wanna give the proxy the limited delegation, which satisfies that

- The proxy can generate the signature on **only one message from two given messages**.
- The signature generated by the proxy is **indistinguishable** from the one by the signer.



# Scenario

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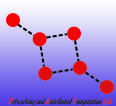
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Extension

- Proxy signature ✘
  - Distinguishable



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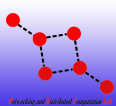
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- Proxy signature ✘
  - Distinguishable
- Proxy re-signature ✘
  - Public key is changed



# Scenario

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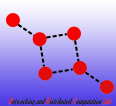
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- Proxy signature ✘
  - Distinguishable
- Proxy re-signature ✘
  - Public key is changed
- Mediated signature ✘
  - The proxy is always involved



# Functionality of 1-out-of-2 signature

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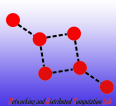
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1-out-of-2 signature is a kind of signature with delegation capability.



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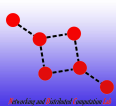
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1-out-of-2 signature is a kind of signature with delegation capability. In particular,

- The proxy **can transform** one of two given partial signatures of the signer into one full signature.



# Functionality of 1-out-of-2 signature

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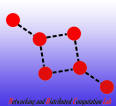
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1-out-of-2 signature is a kind of signature with delegation capability. In particular,

- The proxy **can transform** one of two given partial signatures of the signer into one full signature.
- The proxy can transform **only one** of the two given partial signatures; otherwise, the secret key of the proxy will be **revealed**.





# Definition

## 1-out-of-2 Signature

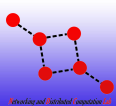
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- $SKeyGen(1^k) \rightarrow (pk_S, sk_S)$ .
- $PKeyGen(1^k) \rightarrow (pk_P, sk_P)$ .
- $PreSign(sk_S, pk_P, (m_0, m_1)) \rightarrow ((\sigma_0, m_0), (\sigma_1, m_1))$ .
- $Trans(\sigma_0, \sigma_1, sk_P) \rightarrow \sigma'_b, (b \in \{0, 1\})$ .
- $Verify((\sigma', m), pk_S) \rightarrow 1 \text{ or } 0$ .
- $Reveal((\sigma_0, \sigma_1), (\sigma'_0, \sigma'_1), pk_P) \rightarrow sk_P$ .



# Security Model—Existential Unforgeability

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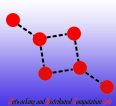
*Setup*  $(pk_S, sk_S), (pk_P, sk_P)$ .

*Queries*

- Secret key oracle  $\mathcal{O}_{Psk}$ .
- Partial signature generation oracle  $\mathcal{O}_{ps}$ .
- Full signature generation oracle  $\mathcal{O}_t$ .

*Forgery* The adversary outputs a full signature  $(\sigma^*, m^*)$ .

- $\text{Verify}((\sigma^*, m^*), pk_S) \rightarrow 1$ .
- $(*, m^*)$  has not been queried to  $\mathcal{O}_t$ .
- $m^*$  has not been queried to  $\mathcal{O}_{ps}$  or  $\mathcal{O}_{Psk}$  has not been queried.



# Security Model—Confidentiality

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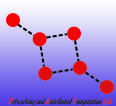
Extension

*Setup* Identical to that in the game for Existential Unforgeability.

*Queries*

- Secret key oracle  $\mathcal{O}_{Ssk}$ .
- Partial signature generation oracle  $\mathcal{O}_{ps}$ .
- Full signature generation oracle  $\mathcal{O}_t$ .

*Output* The adversary wins if he/she outputs the proxy's secret key  $sk_P$ .



# Our proposal—one-time signature method

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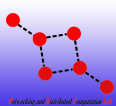
Extension

It works in a finite cyclic group  $G = \langle g \rangle$  with prime order  $p$ .

- SKeyGen:  $X = g^x \in G, x \in \mathbb{Z}_p^*$ .
- PKeyGen:  $Y = g^y \in G, y \in \mathbb{Z}_p^*$ .
- PreSign:  $(x, Y, m_0, m_1)$ 
  - The proxy sends  $A = g^a$  to the signer, where  $a$  is a random number from  $\mathbb{Z}_p^*$ .
  - On receiving  $A$ , the signer computes two partial signatures on  $m_0, m_1$  as follows. For  $(b' = 0, 1)$

$$\begin{aligned}R_{b'} &= (Y^{H_1(Y||A||b')} \cdot A) \cdot g^{r_{b'}}, \\S_{b'} &= r_{b'} + H_2(m_{b'}||R_{b'}) \cdot x \pmod p,\end{aligned}$$

- where  $r_{b'}, (b' = 0, 1)$  are random numbers from  $\mathbb{Z}_p^*$ .
- The signer sends  $(R_{b'}, S_{b'}, b'), (b' = 0, 1)$  to the proxy.



# Our proposal

## 1-out-of-2 Signature

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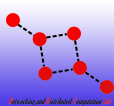
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- **Trans:** On input  $(R_{b'}, S_{b'}, m_{b'})$ ,  $(b' = 0, 1)$ ,  $a, y$ , it outputs  $(R'_b, S'_b, b)$ ,  $(b \in \{0, 1\})$ :  
$$R'_b = R_b, \quad S'_b = S_b + (y \cdot H_1(Y || g^a || b) + a) \bmod p.$$
- **Verify:** On input  $(R', S', m)$ ,  $X$ , it outputs 1 if  $g^{S'} = R' \cdot X^{H_2(m || R')}$  holds; otherwise, it outputs 0.
- **Reveal:** On input  $(R_{b'}, S_{b'}, b')$ ,  $(b' = 0, 1)$ ,  $(R'_{b'}, S'_{b'}, b')$ ,  $(b' = 0, 1)$ ,  $A, Y$ , it outputs  $y$ .

$$\begin{cases} S'_0 - S_0 = y \cdot H_1(Y || A || 0) + a \bmod p, \\ S'_1 - S_1 = y \cdot H_1(Y || A || 1) + a \bmod p. \end{cases}$$



# Security analysis

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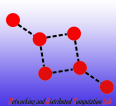
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## Theorem

*The above proposal is existentially unforgeable and confidential in the random oracle model based on the DL assumption.*



# 1-out-of- $k$ signature

## 1-out-of-2 Signature

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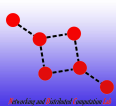
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- In algorithm `PreSign`, the signer returns  $k$  partial signatures to the proxy, other algorithms remain the same.



# Strong 1-out-of-2 signature

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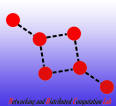
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The adversary has the **unlimited** computational power while the signer or the proxy only has the polynomially bounded power.





# Strong 1-out-of-2 signature scheme—fail-stop signature method

## 1-out-of-2 Signature

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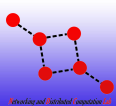
Extension

- **SKeyGen**: The signer chooses  $4\ell + 2$  random numbers  $x_1^{(0)}, x_2^{(0)}, \{x_1^{(i)}, x_2^{(i)}, x_3^{(i)}, x_4^{(i)}\}_{i=1}^{\ell}$  from  $Z_p^*$ , and computes  $X^{(0)} = g^{x_1^{(0)}} h^{x_2^{(0)}}$  and  $X_0^{(i)} = g^{x_1^{(i)}} h^{x_3^{(i)}}$ ,  $X_1^{(i)} = g^{x_2^{(i)}} h^{x_4^{(i)}}$  for  $(i = 1, \dots, \ell)$ . The public key is

$$\mathcal{X} = (X^{(0)}, \{X_0^{(i)}, X_1^{(i)}\}_{i=1}^{\ell}),$$

and the secret key is

$$\mathbb{X} = (x_1^{(0)}, x_2^{(0)}, \{x_1^{(i)}, x_2^{(i)}, x_3^{(i)}, x_4^{(i)}\}_{i=1}^{\ell}).$$



# Strong 1-out-of-2 signature scheme

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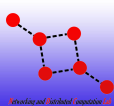
Extension

- PKeyGen: The proxy chooses  $2\ell + 2$  random numbers  $\{y_1^{(i)}, y_2^{(i)}\}_{i=0}^{\ell}$  from  $Z_p^*$ , and computes  $Y_i^{(0)} = g^{y_1^{(i)}} h^{y_2^{(i)}}$  for  $(i = 0, \dots, \ell)$ . The public key is

$$\mathcal{Y} = \{Y^{(i)}\}_{i=0}^{\ell},$$

and the secret key is

$$\mathcal{y} = \{y_1^{(i)}, y_2^{(i)}\}_{i=0}^{\ell}.$$



# Strong 1-out-of-2 signature scheme

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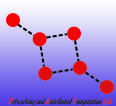
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- PreSign: On input the signer's secret key  $\mathbb{x} = (x_1^{(0)}, x_2^{(0)}, \{x_1^{(i)}, x_2^{(i)}, x_3^{(i)}, x_4^{(i)}\}_{i=1}^{\ell})$ , the proxy's public key  $\mathcal{Y} = \{Y^{(i)}\}_{i=0}^{\ell}$ , and two messages  $m_0, m_1$  from the message space, the partial signature generation algorithm is performed as follows.
  - Assume that it is the  $\kappa$ -th time, then the signer computes two partial signatures on  $m_0, m_1$  as follows. For  $(b' = 0, 1)$

$$\begin{aligned}\sigma_{b'}^{(1)} &= x_1^{(0)} + H_2(m_{b'} || \kappa) \cdot x_{1+b'}^{(\kappa)} \bmod p, \\ \sigma_{b'}^{(2)} &= x_2^{(0)} + H_2(m_{b'} || \kappa) \cdot x_{3+b'}^{(\kappa)} \bmod p.\end{aligned}$$

- The signer sends  $(\kappa, b', \sigma_{b'}^{(1)}, \sigma_{b'}^{(2)})$ ,  $(b' = 0, 1)$  to the proxy.



# Strong 1-out-of-2 signature scheme

## 1-out-of-2 Signature

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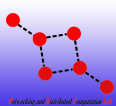
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- Trans: On input two partial signatures  $(\kappa, b', \sigma_{b'}^{(1)}, \sigma_{b'}^{(2)})$ ,  $(b' = 0, 1)$ , the 1-out-of-2 full signature generation algorithm outputs a full signature  $(\kappa, b, \sigma_b^{(1)'}, \sigma_b^{(2)'})$ ,  $(b \in \{0, 1\})$ .

$$\begin{aligned}\sigma_b^{(1)'} &= \sigma_b^{(1)} + (y_1^{(0)} + y_1^{(\kappa)} \cdot H_1(\kappa||b)) \bmod p, \\ \sigma_b^{(2)'} &= \sigma_b^{(2)} + (y_2^{(0)} + y_2^{(\kappa)} \cdot H_1(\kappa||b)) \bmod p.\end{aligned}$$



# Strong 1-out-of-2 signature scheme

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1-out-of-2  
signature

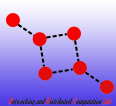
Our proposal

Extension

- **Verify:** On input a full signature  $(\kappa, b, \sigma^{(1)'}, \sigma^{(2)'}, m)$ , the signer's public key  $\mathcal{X}$ , it outputs 1 if

$$g^{\sigma^{(1)'}} \cdot h^{\sigma^{(2)'}} = (X^{(0)} \cdot Y^{(0)} \cdot (Y^{(\kappa)})^{H_1(\kappa||b)}) \cdot (X_b^{(\kappa)})^{H_2(m||\kappa)}$$

holds; otherwise, it outputs 0.



# Strong 1-out-of-2 signature scheme

## 1-out-of-2 Signature

Miroslaw  
Kutyłowski<sup>1</sup>  
and  
Jun Shao<sup>2</sup>

What's  
1-out-of-2  
Signature

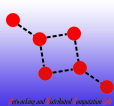
Definitions of  
1-out-of-2  
signature

Our proposal

Extension

- **Reveal:** On input two partial signatures  $(\kappa, b', \sigma_{b'}^{(1)}, \sigma_{b'}^{(2)})$ ,  $(b' = 0, 1)$ , two full signatures  $(\kappa, b', \sigma_{b'}^{(1)'}, \sigma_{b'}^{(2)'})$ ,  $(b' = 0, 1)$ , and the proxy's public key  $\mathcal{Y}$ , it outputs the proxy's secret key  $(y_1^{(0)}, y_2^{(0)})$  by the following equations.

$$\begin{cases} \sigma_0^{(1)'} - \sigma_0^{(1)} = y_1^{(0)} + y_1^{(\kappa)} \cdot H_1(\kappa||0) \bmod p, \\ \sigma_0^{(2)'} - \sigma_0^{(2)} = y_2^{(0)} + y_2^{(\kappa)} \cdot H_1(\kappa||0) \bmod p, \\ \sigma_1^{(1)'} - \sigma_1^{(1)} = y_1^{(0)} + y_1^{(\kappa)} \cdot H_1(\kappa||1) \bmod p, \\ \sigma_1^{(2)'} - \sigma_1^{(2)} = y_2^{(0)} + y_2^{(\kappa)} \cdot H_1(\kappa||1) \bmod p, \end{cases}$$



# Strong 1-out-of-2 signature scheme

## 1-out-of-2 Signature

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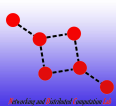
What's  
1-out-of-2  
Signature

Definitions of  
1-out-of-2  
signature

Our proposal

Extension

- **Stop-fail:** With a forgery  $(\kappa^*, b^*, (\sigma^{(1)'})^*, (\sigma^{(2)'})^*, m^*)$ , the proxy and the signer do the following steps: The signer generates a partial signature  $(\kappa^*, b^*, \sigma^{(1)}, \sigma^{(2)}, m^*)$ , and sends it to the proxy with  $(\kappa^*, b^*, (\sigma^{(1)'})^*, (\sigma^{(2)'})^*, m^*)$ . Upon receiving the data from the signer, the proxy first checks the validity of the received data. If it is valid, then the proxy computes and outputs the full signature  $(\kappa^*, b^*, \sigma^{(1)'}, \sigma^{(2)'}, m^*)$ ; otherwise, the proxy aborts the algorithm.



# Security analysis

## 1-out-of-2 Signature

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Jun Shao<sup>2</sup>

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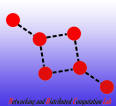
Our proposal

Extension

## Theorem

*The strong 1-out-of-2 signature scheme is existentially unforgeable and confidential in the standard model based on the DL assumption.*





# Future work

## 1-out-of-2 Signature

Mirosław  
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and  
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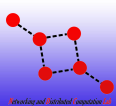
What's  
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Our proposal

Extension

- Non-interactive
- $t$ -out-of- $n$
- ...



## 1-out-of-2 Signature

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Our proposal

Extension

Thank you for your attention!