



Protection of  
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# Protection of Digital Images from Personal Identity Documents

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# Motivation

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- Electronic layer of e-ID may store a high resolution face image of the document holder – more detailed than the image printed on the document.



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- Electronic layer of e-ID may store a high resolution face image of the document holder – more detailed than the image printed on the document.
- The strategy applied in particular by biometric passports is to present not only raw data, but also a signature of the document issuer for those data.



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- The strategy applied in particular by biometric passports is to present not only raw data, but also a signature of the document issuer for those data.

*In this way during an inspection we may become convinced that the image presented originates from the document issuer and has not been replaced even if chip security of e-ID has been broken.*



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- The strategy applied in particular by biometric passports is to present not only raw data, but also a signature of the document issuer for those data.  
*In this way during an inspection we may become convinced that the image presented originates from the document issuer and has not been replaced even if chip security of e-ID has been broken.*
- Once the signed data is shown to a second party, the owner of e-ID has no further control over who has access to it. In particular, this data can be sold to third parties.



# System goals

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- Once a face image is presented by an e-ID, then a customized signature **of the document issuer** is attached.



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- Once a face image is presented by an e-ID, then a customized signature **of the document issuer** is attached.
- The signature indicates the recipient of the signature.



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- Once a face image is presented by an e-ID, then a customized signature **of the document issuer** is attached.
- The signature indicates the recipient of the signature.
- Issuer's signing key is not copied on the e-ID!





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- Once a face image is presented by an e-ID, then a customized signature **of the document issuer** is attached.
- The signature indicates the recipient of the signature.
- Issuer's signing key is not copied on the e-ID!
- The authority issuing the e-ID documents cannot create clone documents and customized signatures in order to accuse a certain party for violations of personal data protection.



# Assumptions about e-ID chips

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- We assume that keys generated privately on the chip can be read by the e-ID issuer as long as the key generation process takes place in environment controlled by the issuer.



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- We assume that keys generated privately on the chip can be read by the e-ID issuer as long as the key generation process takes place in environment controlled by the issuer.
- However, keys generated on the chip when the e-ID is in control of the owner are neither predictable for the e-ID issuer nor they leak from the e-ID.



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The assumptions above reflects the setting where:

- the chip vendor does not collude with the document issuer,



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- However, keys generated on the chip when the e-ID is in control of the owner are neither predictable for the e-ID issuer nor they leak from the e-ID.

The assumptions above reflects the setting where:

- the chip vendor does not collude with the document issuer,
- the issuer has access to technologies that with physical access to the chip may break security means on the chip and can access all relevant data on it.



# Solutions

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- Two protocols are presented in the paper:
  - a symmetric one,
  - an asymmetric one.



# Solutions

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- Two protocols are presented in the paper:
  - a symmetric one,
  - an asymmetric one.
- The first one is well suited to weak devices (like e-passports with BAC), but resolution of indication of signature recipient is limited (to say  $2^{10}$  classes of recipients).
- The second one requires more capable chips (like e-passports with EAC), but the resolution mentioned above is unlimited.



# The Asymmetric Solution

## The Main Mechanism

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- As usually, the datagroups  $D$  and the signature of the document issuer are presented to the verifier (*for simplicity we assume that all datagroups are revealed to a verifier*).





# The Asymmetric Solution

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- But the chip of e-ID attaches a tag to the pair: (the data groups, the signature).



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- As usually, the datagroups  $D$  and the signature of the document issuer are presented to the verifier (*for simplicity we assume that all datagroups are revealed to a verifier*).
- But the chip of e-ID attaches a tag to the pair: (the data groups, the signature).
- The point is that without the tag signature verification is infeasible, and that the tag indicates the intended verifier.



# The Asymmetric Solution

The Main Building Block - Schnorr-like Proof of EDL

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Let  $\langle g \rangle$  be of prime order  $q$ . Let DDHP be hard in  $\langle g \rangle$ .

The prover performs the following steps:

- 1 generate  $r$  at random,
- 2  $k := g^r, \ell := h^r$ ,
- 3  $e := H(k, \ell, g, h, a, b, m)$ , where  $m$  is some message
- 4  $s := r + ex \text{ mod } q$ ,
- 5 send  $(e, s)$  to the verifier.

The verifier performs the following steps:

- 1  $k' := g^s / a^e$ ,
- 2  $\ell' := h^s / b^e$ ,
- 3  $e' := H(k', \ell', g, h, a, b, m)$ ,
- 4 return ok if  $e = e'$ .



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- The system is supported by a card management system called below CAMS.
- We refer also to standard protocols for chip authentication (Chip Authentication or ChA) and authenticating terminals (Terminal Authentication or TA) [BSI TR-03110].



# The Protocol

## Document personalization

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For each single identity document the following steps are executed by issuing authority:



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For each single identity document the following steps are executed by issuing authority:

- 1 All but two data groups for the e-ID are completed in advance, and are stored in some registry on the side of CAMS.



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- 2** The data groups are copied to the chip of e-ID.



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- 2** The data groups are copied to the chip of e-ID.
- 3** The private key and the corresponding public key for ChA are generated by the e-ID chip.





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- 2** The data groups are copied to the chip of e-ID.
- 3** The private key and the corresponding public key for ChA are generated by the e-ID chip.
- 4** The ChA public key is copied to the data groups (i.e., to a copy stored locally on the e-ID chip as well to a copy stored in the registry of CAMS).



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- 4** The ChA public key is copied to the data groups (i.e., to a copy stored locally on the e-ID chip as well to a copy stored in the registry of CAMS).
- 5** The e-ID chip enters a “red” state



# The Protocol

## Document personalization - results

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- The data groups are still not authenticated by the issuing authority.



# The Protocol

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- The data groups are still not authenticated by the issuing authority.
- The e-ID is in a “red” state, which means that all functions of the chip are blocked – only Terminal Authentication and Chip Authentication with terminals of CAMS are allowed.



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## Document personalization - results

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- The data groups are still not authenticated by the issuing authority.
- The e-ID is in a “red” state, which means that all functions of the chip are blocked – only Terminal Authentication and Chip Authentication with terminals of CAMS are allowed.
- When the e-ID is in hands of its owner, it must be unblocked.



# The Protocol

Unlocking the chip - Phase I

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In a private environment the owner connects to a service of CAMS and after execution of TA+ChA:



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In a private environment the owner connects to a service of CAMS and after execution of TA+ChA:

- 1 The e-ID chip generates its private key  $\tilde{x}$  for tagging, and computes  $\tilde{a} = g^{\tilde{x}}$ , where  $g$  is fixed in the system (the same for all users).



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## Unblocking the chip - Phase I

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- 2 Key  $\tilde{a}$  is written in the remaining empty data group, both in the e-ID chip and in the CAMS registry.





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- 3 The e-ID chip and CAMS each compute  $\tilde{h} = H_g(D)$ , where  $H_g$  is a hash function with the image included in the group generated by  $g$ .



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- 4 The e-ID chip computes  $\tilde{b} = \tilde{h}^{\tilde{x}}$  and sends  $\tilde{b}$  to CAMS.



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- 4 The e-ID chip computes  $\tilde{b} = \tilde{h}^{\tilde{x}}$  and sends  $\tilde{b}$  to CAMS.
- 5 The e-ID chip and CAMS execute the Schnorr-like ZKP for equality of discrete logarithms for  $\tilde{a}, \tilde{b}$  and the corresponding bases  $g, \tilde{h}$  ( $m$  is chosen to be the string "CAMS").



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- 6 The e-ID chip enters a “yellow” state.



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## Phase I – Results

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We have the following mappings:

$$g \longrightarrow \tilde{a} = g^{\tilde{x}}$$

$$\tilde{h} \longrightarrow \tilde{b} = \tilde{h}^{\tilde{x}}$$

where

- $g$  is fixed for all users
- $\tilde{h}$  is calculated from the data groups:  $\tilde{h} = H_g(D)$
- $\tilde{a}$  is written in  $D$



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## Unblocking the chip - Phase II

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On the side of CAMS:



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## On the side of CAMS:

- 1 User's data groups from CAMS's registry are transferred, together with the ZKP of EDL, to the document issuing authority.



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## Unlocking the chip - Phase II

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### On the side of CAMS:

- 1 User's data groups from CAMS's registry are transferred, together with the ZKP of EDL, to the document issuing authority.
- 2 The document issuing authority verifies the proof and generates a signature  $Sign(\tilde{b})$  under  $\tilde{b}$ .





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- 3  $Sign(\tilde{b})$  is transferred back to CAMS's registry.



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## On the side of e-ID:



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## On the side of e-ID:

- 1 If an e-ID is in the "yellow" state, then any time the e-ID is used it tells the middle-ware to connect to CAMS's service to fetch  $Sign(\tilde{b})$ .



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### On the side of e-ID:

- 1 If an e-ID is in the "yellow" state, then any time the e-ID is used it tells the middle-ware to connect to CAMS's service to fetch  $Sign(\tilde{b})$ .
- 2 Once  $Sign(\tilde{b})$  is fetched, the e-ID switches from the "yellow" state to the "green" one ("regular usage").



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## Phase II – Results

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where

- $g$  is fixed for all users
- $\tilde{h}$  is calculated from the data groups:  $\tilde{h} = H_g(D)$
- $\tilde{a}$  is written in  $D$
- The e-ID has  $Sign(\tilde{b})$  under  $\tilde{b}$ .



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## Data Group Authentication

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To execute this part the e-ID must be in “green” state. After completion of TA+ChA:



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To execute this part the e-ID must be in “green” state. After completion of TA+ChA:

- 1 The e-ID chip sends  $D$  and  $Sign(\tilde{b})$  to the terminal.



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To execute this part the e-ID must be in “green” state. After completion of TA+ChA:

- 1 The e-ID chip sends  $D$  and  $Sign(\tilde{b})$  to the terminal.
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- 3 The e-ID chip computes  $\tilde{h} = H_g(D)$  and  $\tilde{b} = \tilde{h}^x$  and sends  $\tilde{b}$  to the terminal (now both sides know the tuple  $(\tilde{a}, \tilde{b}, g, \tilde{h})$  and  $Sign(\tilde{b})$ , but the link between  $\tilde{h}$  and  $\tilde{b}$  must be proven by the e-ID chip).



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- 4 Both parties execute ZKP for EDL for  $\tilde{a}, \tilde{b}$  and the corresponding bases  $g, \tilde{h}$ . Schnorr-like protocol is used for  $m$  being a string identifying the verifier.



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- The exponentiation  $\tilde{h}^{\tilde{x}}$ , where  $\tilde{h} = H_g(D)$ , resembles BLS signature scheme. However, if  $\langle g \rangle$  would be a pairing friendly group, no ZKP-EDL would be necessary, because equality could immediately be checked with pairing (**but we have assumed that DDHP is hard in  $\langle g \rangle$** ).

Thus augmenting the exponentiation with ZKP-EDL we use a kind of an analog of BLS signature scheme in pairing unfriendly groups.



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Thus augmenting the exponentiation with ZKP-EDL we use a kind of an analog of BLS signature scheme in pairing unfriendly groups.

- Since  $D$  is of the form  $(g^{\tilde{x}}, M)$ , where  $M$  are some data, we obtain a kind of a self-signed certificate of the public key  $\tilde{a} = g^{\tilde{x}}$ .

The document issuing authority makes signature  $Sign(\tilde{b})$  under the BLS-like “signature” value  $\tilde{b} = \tilde{h}^{\tilde{x}}$ .



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The document issuing authority makes signature  $Sign(\tilde{b})$  under the BLS-like “signature” value  $\tilde{b} = \tilde{h}^{\tilde{x}}$ .

- **Problem:** *is it feasible to change  $M$  and tune  $\tilde{x}$  accordingly in such a way that  $\tilde{b}$  remains unchanged?*



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- When we try to change  $M$  to  $M'$  we search for  $x' \in \mathbb{Z}_q^*$  yielding a collision:

$$\tilde{b}^{(x')^{-1}} = H_g(g^{x'}, M').$$



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- Probability of such an event is not greater than probability of the following collision

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where  $x', y$  could be independently chosen.



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- Probability of such an event is not greater than probability of the following collision

$$\tilde{b}^{(x')^{-1}} = H_g(y, M'),$$

where  $x', y$  could be independently chosen.

- But the latter collision occurs no more frequently than the collision

$$\tilde{b}^{(x')^{-1}} = H_g(\tilde{M}),$$

where  $\tilde{M}$  could be any bitstring.





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In the random oracle model for  $H_g$  probability of the last event results from [the birthday paradox in two rooms setting](#). Let fix parameter  $\gamma \in (0, 1)$ :



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In the random oracle model for  $H_g$  probability of the last event results from [the birthday paradox in two rooms setting](#). Let fix parameter  $\gamma \in (0, 1)$ :

- Provided that in each single choice of  $(x', \tilde{M})$  an element  $\tilde{b}^{(x')^{-1}} \in \text{Im}(H_g)$ , the number of choices  $(x', \tilde{M})$  yielding the collision with probability no smaller than  $\gamma$  is equal to  $c_\gamma \cdot \sqrt{|\text{Im}(H_g)|}$ , where constant  $c_\gamma$  is dependent of  $\gamma$ .



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- Since  $x', \tilde{M}$  could be chosen independently, the expected number of choices of  $(x', \tilde{M})$  to obtain the collision with probability no smaller than  $\gamma$ , equals in the random oracle model for  $H_g$  to

$$\frac{c_\gamma \cdot \sqrt{|\text{Im}(H_g)|}}{\Pr\left(\tilde{b}^{(x')^{-1}} \in \text{Im}(H_g)\right)}.$$



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# Thanks for your attention!

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